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E. G. Santos, S. R. de Oliveira Neto, E. J. Kinast, J. B. M. da Cunha, Olivier Isnard, et al.. Magnetic phases of the quasi-two-dimensional compounds  $\text{FexCo}_{1-x}\text{Ta}_2\text{O}_6$ . *Journal of Physics: Condensed Matter*, 2010, 22, pp.6004. 10.1088/0953-8984/22/49/496004 . hal-00978118

**HAL Id: hal-00978118**

**<https://hal.science/hal-00978118>**

Submitted on 26 Apr 2014

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# Magnetic phases of the quasi-two-dimensional compounds $\text{Fe}_x\text{Co}_{1-x}\text{Ta}_2\text{O}_6$

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**Abstract.** We report new results about magnetic properties of the  $\text{Fe}_x\text{Co}_{1-x}\text{Ta}_2\text{O}_6$  series of compounds. Using essentially neutron diffraction and magnetic measurements we study in more detail the low- $x$  limit of the temperature vs.  $x$  phase diagram, where a new bicritical point is observed. The complete phase diagram shows three different magnetic phases at low temperature, for high, intermediate and very low iron content. These phases consist of distinct antiferromagnetic orderings, characterized by different pairs of propagation vectors. We obtain information about the intraplane exchange interactions by fitting a high-temperature series of the magnetic susceptibility. Here we improve on a previously employed model, showing that the model must include two non-equivalent next-nearest-neighbor interactions in order to allow for in-plane magnetic orderings consistent with the neutron-diffraction results.

PACS numbers: 75.25.-j, 75.30.Cr, 75.30.Et, 75.30.Gw, 75.47.Lx

## 1. Introduction

The  $ATa_2O_6$  trirutile compounds with  $A = \text{Co}$ ,  $\text{Ni}$  or  $\text{Fe}$  present a rich variety of magnetic phases, dominated by low-dimensionality effects. Since the original investigation of the magnetic properties of  $\text{FeTa}_2\text{O}_6$  by Eicher and coworkers [1], many studies have followed, not only using magnetic measurements [2] but also Mössbauer spectroscopy [3], and elastic as well as inelastic neutron scattering techniques on powder or single-crystal samples [4, 5]. Magnetic ordering in Co and Ni isotype compounds has also been the subject of complementary investigations [6–10]. Recently, the  $\text{CoTa}_2\text{O}_6$  compound has been reported to exhibit a different magnetic structure [11] than the one previously suggested [8]. In addition to its interesting magnetic properties,  $\text{NiTa}_2\text{O}_6$  has also been found to be an interesting candidate for applications as water-splitting photocatalyst [12]. Bicriticality has been discovered [13] in the  $\text{Fe}_x\text{Co}_{1-x}\text{Ta}_2\text{O}_6$  series

for  $x = 0.46$ , showing another interesting property of these compounds. Studies of magnetic properties have also been reported on  $\text{Fe}_x\text{Ni}_{1-x}\text{Ta}_2\text{O}_6$  compounds [14, 15].

At this point it is worth summarizing the main features of the  $\text{Fe}_x\text{Co}_{1-x}\text{Ta}_2\text{O}_6$  compounds. The entire series crystallizes in the trirutile structure, which is tetragonal with the  $P4_2/mnm$  space group [16]. In such structure,  $\text{Fe}^{2+}$  or  $\text{Co}^{2+}$  cations are located at the corners and center of each unit cell, i.e., at positions  $(0,0,0)$  and  $(1/2, 1/2, 1/2)$ . These cation layers are separated by two layers of  $\text{Ta}^{5+}$ , at positions  $z \sim 1/6$  and  $z' \sim 1/3$  measured along the  $c$  direction. Each cation is surrounded by  $\text{O}^{2-}$  anions occupying the vertexes of an octahedron. The oxygen octahedra are distorted, having a shorter principal axis lying on the  $ab$  plane, and rotating by  $90^\circ$  upon a translation of  $(1/2, 1/2, 1/2)$ . These materials exhibit quasi-two-dimensional magnetic characteristics. They are paramagnetic at room temperature, present short-range magnetic correlations at low temperature ( $\sim 15$  K), as evidenced by a broad maximum of the magnetic susceptibility as a function of temperature, and order antiferromagnetically, with Néel temperatures between 5 and 9.5 K.  $\text{FeTa}_2\text{O}_6$  presents a magnetic structure described by two propagation vectors,  $(1/2, 0, 1/2)$  and  $(0, 1/2, 1/2)$  [1], associated to magnetic ions at the corner and center of the structural unit cell, whose magnetic moments are oriented perpendicularly to one another. In the following we will refer to this structure as AFF (F for Fe). On the other hand,  $\text{CoTa}_2\text{O}_6$  presents a magnetic structure indexed by the propagation vectors  $(\pm 1/4, 1/4, 1/4)$  [11], which we will call AFC (C for Co). A previous study of the  $\text{Fe}_x\text{Co}_{1-x}\text{Ta}_2\text{O}_6$  series [13] showed that the magnetic ordering observed for  $\text{FeTa}_2\text{O}_6$  is stable for high  $x$  values, from 1.0 down to 0.46, while the magnetic structure of  $\text{CoTa}_2\text{O}_6$  is no longer present for iron concentration as low as 10%, where a third phase appears that remains stable up to  $x \sim 0.46$ . This phase is described by the propagation vectors  $(\pm 1/4, 1/4, 0)$ , and will be called AFI (I for Intermediate).

An important point concerning the magnetic phases revealed by neutron diffraction in  $\text{Fe}_x\text{Co}_{1-x}\text{Ta}_2\text{O}_6$  compounds is that they imply the existence of strong magnetic (crystal-field) anisotropy. All magnetic moments lie on the  $ab$  plane, alternating along the directions  $[1, 1, 0]$  and  $[1, \bar{1}, 0]$  from one plane to the next, these easy-axis directions coinciding with the orientation of a shortened principal axis of the oxygen octahedron surrounding each magnetic ion. This  $90^\circ$  rotation of the moments from one magnetic plane to the next follows the corresponding rotation of the octahedra in the trirutile structure. Both the low-dimensional character and the strong in-plane easy-axis anisotropy are very robust features of these compounds. In fact, they are also evident in the paramagnetic phase where the susceptibility data can be fitted to a high-temperature series evaluated for a two-dimensional (2D) Heisenberg model with an in-plane easy axis and competing nearest-neighbor (nn) and next-nearest-neighbor (nnn) exchange interactions [2, 13].

Despite the large amount of information partially summarized above, gaps still exist in our understanding of the magnetism in the  $(\text{Fe}, \text{Co})\text{Ta}_2\text{O}_6$  series. In this paper, we will concentrate on two aspects. First, we will experimentally investigate the stability region of the AFC magnetic phase, and its coexistence with the AFI phase for samples

with very low iron content. Second, we will revisit the 2D model employed for the paramagnetic susceptibility, which, as we will show, needs to be reformulated in order to yield values of exchange interactions that are consistent with the observed in-plane magnetic structures at low temperature.

## 2. Magnetic phases for low iron content

In order to determine more precisely the composition limit between the AFC and AFI magnetic phases, we prepared new powder samples of  $\text{Fe}_x\text{Co}_{1-x}\text{Ta}_2\text{O}_6$ , with  $x = 0.01$ ,  $0.02$ , and  $0.04$ . The samples were prepared as previously described [16]. Sample purity was first checked by x-ray diffraction (XRD) analysis before carrying out magnetic measurements [16] and neutron-diffraction experiments. The XRD analysis has been performed with a Siemens D500 diffractometer installed at the Instituto de Física – UFRGS, in Bragg-Brentano geometry, using  $\text{CuK}_\alpha$  radiation,  $\lambda(K_{\alpha 1}) = 1.54056 \text{ \AA}$  and  $\lambda(K_{\alpha 2}) = 1.54439 \text{ \AA}$ , with scan step of  $0.02^\circ$  and angular  $2\theta$  range from  $10^\circ$  to  $120^\circ$ . Structure parameters were confirmed to be in agreement with those previously obtained for the whole series [13].

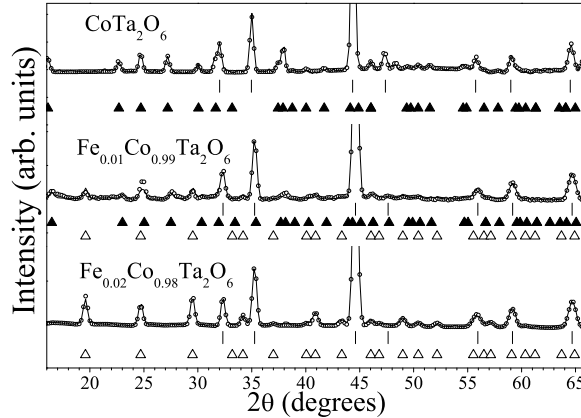
### 2.1. Magnetic measurements

Magnetic measurements were carried using an extraction magnetometer, in a wide temperature range, from 1.5 K to 300 K. Both isothermal magnetization,  $M(H)$ , and temperature-dependent susceptibility,  $\chi(T)$ , have been measured. The  $M(H)$  curves have been recorded in magnetic field ranging from 0 to 100 kOe.  $\chi(T)$  was obtained by field-cooling the samples at a constant magnetic field of 5 kOe, then keeping the field fixed and measuring the magnetization while rising the temperature. Above 50 K, for better accuracy, the values of magnetic susceptibility have been extracted from “Arrot plots” of the isothermal magnetization. In other words,  $1/\chi(T)$  was obtained by extrapolating the linear part of  $H/M$  vs.  $M^2$  curve down to  $M = 0$  [18].

The samples order with an antiferromagnetic structure at low temperatures. We achieved a precise determination of the Néel temperature  $T_N$  by measuring the susceptibility at intervals of 0.2 K in the range from 1.5 to 20 K, and numerically performing the derivative  $\partial(T\chi(T))/\partial T$ , which presents a well defined peak at the transition. The Néel temperature showed a marked reduction from  $x = 0$  to  $x = 0.01$ , and then started to rise again towards the value previously obtained [13] for  $x = 0.1$ . This is similar to what was observed near  $x = 0.46$  [13], and can be interpreted as another bicritical point in the  $T$  vs.  $x$  phase diagram. This interpretation is corroborated by neutron-diffraction experiments, as discussed below.

### 2.2. Neutron diffraction

Neutron-diffraction data were collected with a double-axis, multicounter, high-flux diffractometer (D1B) at the Institute Laue Langevin (ILL), in Grenoble, France,

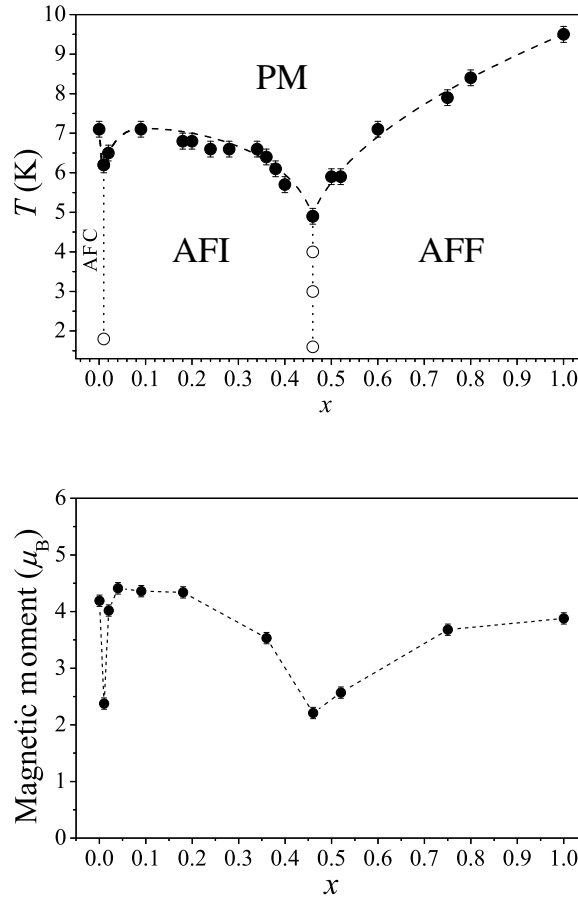


**Figure 1.** Neutron-diffraction spectra showing phase coexistence at  $x = 0.01$  for the  $\text{Fe}_x\text{Co}_{1-x}\text{Ta}_2\text{O}_6$  solid solution. The reflections indicated by solid triangles correspond to the magnetic phase described by propagation vectors  $(\pm 1/4, 1/4, 1/4)$ , while open triangles mark reflections of the phase with propagation vectors  $(\pm 1/4, 1/4, 0)$ . Vertical bars locate structural reflections of the  $P4_2/mnm$  space group. Continuous lines are Rietveld fittings to the data points.

using a wavelength of  $2.52 \text{ \AA}$  selected by a pyrolytic graphite monochromator. In the configuration employed, the D1B resolution was about  $0.3^\circ$  (fwhm), and the multicounter was composed of 400 cells covering a total angular ( $2\theta$ ) range of  $80^\circ$ , from  $5^\circ$  to  $85^\circ$ , with a detector step of  $0.2^\circ$ . The  $2\theta$  range was checked down to  $2^\circ$ , enabling to rule out the possible occurrence of other magnetic Bragg reflections.

We analyzed our neutron-diffraction data using the FULLPROF refinement package [19] in order to extract crystallographic and magnetic parameters. Agreement factors used in this work are defined according to the guidelines of the Rietveld refinement [20]. The neutron scattering lengths used were  $0.5803 \times 10^{-12} \text{ cm}$  for Ta,  $0.9450 \times 10^{-12} \text{ cm}$  for Fe,  $0.2490 \times 10^{-12} \text{ cm}$  for Co, and  $0.5803 \times 10^{-12} \text{ cm}$  for O, values taken from Sears [21].

Figure 1 shows neutron spectra for three samples in the limit of very low iron concentration:  $x = 0$ ,  $0.01$ , and  $0.02$ . We have cut off the intensity scale in order to make the magnetic reflections more visible. The first sample, which is just  $\text{CoTa}_2\text{O}_6$ , is indexed by the propagation vectors of the AFC structure, i.e.,  $(\pm 1/4, 1/4, 1/4)$ . The last one is already completely indexed by the propagation vectors corresponding to the AFI structure,  $(\pm 1/4, 1/4, 0)$ . For the intermediate sample,  $x = 0.01$ , we observe the presence of both kinds of reflections, indicating coexistence of these two magnetic phases. A similar coexistence pattern was observed earlier for concentrations near  $x = 0.46$  [13], in this case involving the AFI and AFF phases. The above result confirms that a bicritical point exists at  $x \simeq 0.01$  in the  $T$  vs.  $x$  phase diagram.



**Figure 2.** Top:  $T$  vs  $x$  phase diagram of the  $\text{Fe}_x\text{Co}_{1-x}\text{Ta}_2\text{O}_6$  series. Solid circles are values of  $T_N$  obtained from magnetic susceptibility measurements, and open circles were obtained from neutron diffraction on the samples that show phase coexistence. Broken lines are guides to the eye. PM stands for the paramagnetic phase, while the ordered phases are labeled as defined in the text. Bottom: Variation of the low-temperature magnetic moment as a function of concentration along the  $\text{Fe}_x\text{Co}_{1-x}\text{Ta}_2\text{O}_6$  solid series, as deduced from refinement of neutron-diffraction data.

### 2.3. Phase diagram

Putting together the information about Néel temperature, obtained from susceptibility measurements, and about the ordered magnetic phases, obtained from neutron diffraction, we can complement the magnetic phase diagram of the  $\text{Fe}_x\text{Co}_{1-x}\text{Ta}_2\text{O}_6$  solid solution, first appearing in [13]. The complete diagram, with two bicritical points, near  $x = 0.01$  and  $x = 0.46$ , is shown in the top panel of figure 2. This  $T$  vs.  $x$  phase diagram correlates well with the variation of low-temperature magnetic moments with composition, as obtained from neutron-diffraction data, which can be seen in the bottom panel of figure 2. It is noticeable that there is a dramatic reduction of magnetic moment for the two compositions exhibiting coexistence of magnetic phases,  $x = 0.46$

and 0.01. An average Fe/Co magnetic moment of only 2.2 and 2.5  $\mu_B$ /atom is obtained for  $x = 0.46$  and 0.01, respectively. This is to be compared with 3.8  $\mu_B$  for  $\text{FeTa}_2\text{O}_6$  and about 4  $\mu_B$  in  $\text{CoTa}_2\text{O}_6$  [10,11]. This difference can possibly be attributed to frustration occurring at interfaces of the coexisting phases.

### 3. Two-dimensional model revisited

Our previous discussion makes it clear that the  $\text{Fe}_x\text{Co}_{1-x}\text{Ta}_2\text{O}_6$  compounds present three-dimensional AF ordering at low temperatures. Nevertheless, their crystal structure, low values of  $T_N$ , and overall shape of the magnetic susceptibility [13] provide strong evidence of quasi-two-dimensional characteristics. Thus, it is reasonable to expect that a purely two-dimensional model would be sufficient to describe their high-temperature behavior. Such a model must take into account the observed strong crystal-field anisotropy, and include competing exchange interactions, since the in-plane magnetic ordering is not a Néel state.

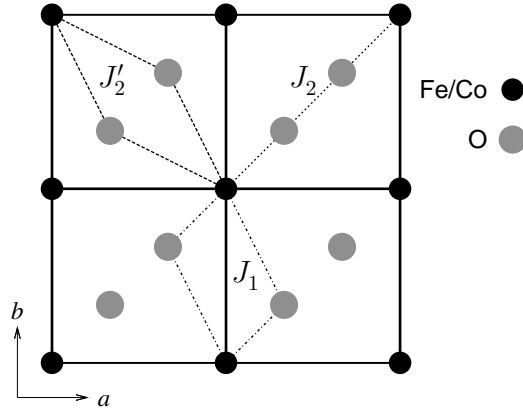
The first model to show some success in interpreting the susceptibility behavior in  $\text{FeTa}_2\text{O}_6$  was a two-dimensional anisotropic Heisenberg model proposed by Muraoka *et al.* [2]. It involves nearest-neighbor (nn) and next-nearest-neighbor (nnn) exchange interactions, and is defined by the Hamiltonian

$$\begin{aligned} \mathcal{H} = & -2J_1 \sum_{\langle ij \rangle}^{\text{nn}} \mathbf{S}_i \cdot \mathbf{S}_j - 2J_2 \sum_{\langle ij \rangle}^{\text{nnn}} \mathbf{S}_i \cdot \mathbf{S}_j \\ & - D \sum_i S_{iz}^2 - \mu_B \sum_i (g_{\parallel} H_z S_{iz} + g_{\perp} H_x S_{ix}). \end{aligned} \quad (1)$$

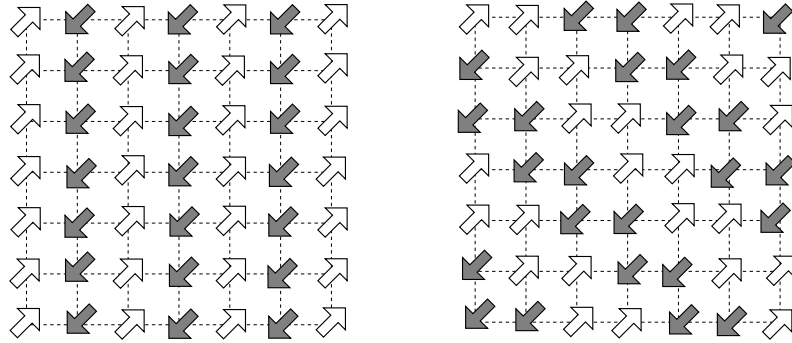
The first two terms describe exchange interactions between spins  $\mathbf{S}_i$  and  $\mathbf{S}_j$  occupying, respectively, nn and nnn lattice sites,  $J_1$  and  $J_2$  being the corresponding exchange constants. A single  $J_2$  has been used in [2] despite the existence of two nonequivalent exchange paths, sketched in figure 3 (labelled by  $J_2$  and  $J_2'$ ), as pointed out by Hague *et al.* [5]. In the third term, where  $D$  measures the anisotropy strength, the easy axis  $z$  (in spite of this notation) lies on the  $ab$  plane, along the direction  $[1, 1, 0]$  or  $[1, \bar{1}, 0]$ , as discussed before. The last term accounts for the effect of an applied magnetic field, with anisotropic  $g$ -factor.

Thanks to our knowledge about the magnetically ordered structures, obtained through neutron diffraction as described in the previous sections, we can check whether the observed spin configurations are consistent with that model. Even though the model is strictly two-dimensional, we should expect in-plane interactions to be dominant in determining the spin configurations on the  $ab$  plane.

Two in-plane spin structures appear in the  $(\text{Fe},\text{Co})\text{Ta}_2\text{O}_6$  system, one for the Fe-rich samples and one for the Co-rich ones, shown in figure 4. The structure observed in Fe-rich samples is characterized by ferromagnetic lines along the  $a$  (or  $b$ ) direction which alternate antiferromagnetically along the transverse direction. This structure has been denominated *super-antiferromagnetic* in the context of the planar Ising model [24], and we will refer to it as SAF1. The structure appearing for Co-rich samples is a different



**Figure 3.** Superexchange paths between nearest and next-nearest neighbors on a magnetic  $ab$  plane (adapted from [5]).

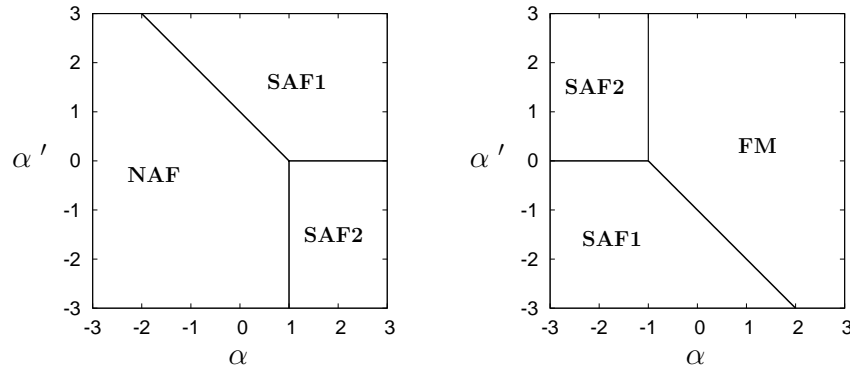


**Figure 4.** Spin patterns on the  $ab$  plane observed in the  $(\text{Fe},\text{Co})\text{Ta}_2\text{O}_6$  system. Left: Fe-rich samples (SAF1). Right: Co-rich samples (SAF2). For clarity, we represent opposite spins in different shades.

kind of super-antiferromagnetic ordering, which we will call SAF2, characterized by pairs of ferromagnetic lines along the diagonal direction perpendicular to the easy axis, which alternate antiferromagnetically along the easy axis. If we make a simple balance of exchange couplings for the bonds connecting each spin to its nearest and next-nearest neighbors on the plane, we easily see that (i) nn interactions are frustrated for both structures, and (ii) nnn interactions are also frustrated in the SAF2 structure, whose energy balance amounts to zero. This structure, then, could never be stable against SAF1. However, the energy of SAF2 would not sum to zero if we allowed for two distinct nnn couplings, as implied from figure 3. Allowing for different  $J_2$  and  $J'_2$ , respectively along the easy axis (dotted line in figure 3) and perpendicular to it, we now analyze the relative stability of the SAF1 and SAF2 structures, also in comparison to the Néel AF ordering (NAF) and the ferromagnetic (FM) state. The ground-state energy per spin in each case (leaving aside the spin value) can be written as

$$\varepsilon_{\text{SAF}} = 2(J_2 + J'_2), \quad \varepsilon_{\text{NAF}} = 4J_1 - 2(J_2 + J'_2),$$





**Figure 5.** Phase diagrams on the  $\alpha\alpha'$  plane for fixed  $J_1 < 0$  (left) and  $J_1 > 0$  (right).

$$\varepsilon_{\text{D2SAF}} = 2(J_2 - J'_2), \quad \varepsilon_{\text{FM}} = -4J_1 - 2(J_2 + J'_2). \quad (2)$$

Defining  $\alpha \equiv J_2/J_1$  and  $\alpha' \equiv J'_2/J_1$ , we can construct the phase diagrams shown in figure 5. There we can see that the SAF2 ordering is not stable along the line  $\alpha' = \alpha$ . Thus, the simplified model of equation (1) cannot account for the magnetic structure observed in Co-rich samples. Nevertheless, a fitting of the susceptibility data to the corresponding high-temperature series up to order  $T^{-4}$  has been done before [13] for the entire  $(\text{Fe},\text{Co})\text{Ta}_2\text{O}_6$  series, with seemingly reasonable results, consistent with the ones originally obtained for  $\text{FeTa}_2\text{O}_6$  [2]. The problem with such a fitting is that the number of parameters of the Hamiltonian that are being determined exceeds the number of free adjustable parameters, since we do not have access to individual components of the susceptibility tensor in the case of powder samples. With model (1) one has to determine the values of five parameters ( $J_1$ ,  $J_2$ ,  $D$ ,  $g_{\parallel}$ , and  $g_{\perp}$ ) from four coefficients of the high-temperature series. The result is then highly dependent on the initial values, and many different sets of parameters give comparable fittings.

We have just concluded that we need to take into account one extra parameter,  $J'_2$ . This makes the situation even worse, since deriving terms beyond fourth order in the high-temperature series is a huge task. However, thanks to the strong easy-axis anisotropy observed for the whole series of compounds, it might be reasonable to utilize an Ising model. With this assumption, we keep only terms involving the  $z$  component of spin operators in equation (1) and drop the anisotropy term, writing the Hamiltonian as

$$\begin{aligned} \mathcal{H} = & -2J_1 \sum_{\langle ij \rangle}^{\text{nn}} S_i^z S_j^z - 2J_2 \sum_{\langle ij \rangle}^{\text{nn}\parallel} S_i^z S_j^z \\ & - 2J'_2 \sum_{\langle ij \rangle}^{\text{nn}\perp} S_i^z S_j^z - gH_z \sum_i S_i^z, \end{aligned} \quad (3)$$

where  $\parallel$  and  $\perp$  are relative to the anisotropy axis. Notice that by assuming an effective Ising model the only allowed values of  $S_i^z$  are  $\pm S$ , even though we are dealing with  $S > 1/2$ .

We are now left with four parameters: three exchange constants and one  $g$ -factor. Writing the susceptibility series as

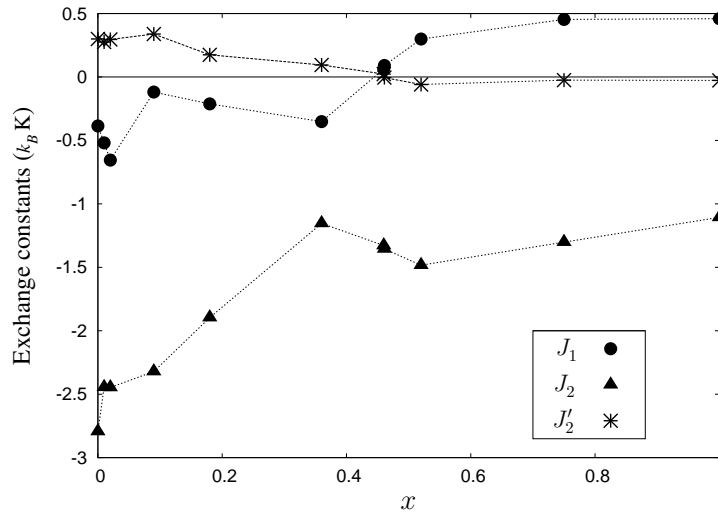
$$\chi = \frac{c}{T} \left( 1 + \frac{a_1}{T} + \frac{a_2}{T^2} + \frac{a_3}{T^3} + \dots \right), \quad (4)$$

we recalculated the four coefficients  $c$ ,  $a_1$ ,  $a_2$ , and  $a_3$  in terms of the parameters  $J_1$ ,  $J_2$ ,  $J'_2$ , and  $g$  of equation (3). A detailed revision of high-temperature series expansions would be out of place here. We just mention the basic aspects of the method. The susceptibility is evaluated as the second derivative of the free energy with respect to the applied magnetic field in the limit where this field goes to zero. The free energy, in turn, is related to the partition function, whose expansion in powers of  $1/T$  involves averages of increasingly higher powers of the Hamiltonian. These averages are evaluated at infinite temperature, i.e., with equally probable spin states. Employing this procedure with the model of equation (3), we obtain the relations listed below.

$$\begin{aligned} c &= g^2 \mu_B^2 S^2 / k_B, \\ a_1 &= 4 S^2 (2J_1 + J_2 + J'_2), \\ a_2 &= 8 S^4 [6J_1^2 + J_2^2 + J'^2_2 + 8J_1(J_2 + J'_2) + 4J_2J'_2], \\ a_3 &= \frac{8}{3} S^6 [104 J_1^3 + 4(J_2^3 + J'^3_2) + 96 J_1(J_2^2 + J'^2_2 + 6J_2J'_2) \\ &\quad + 40(J_2^2J'_2 + J_2J'^2_2) + 198 J_1^2(J_2 + J'_2)]. \end{aligned} \quad (5)$$

Equations (4) and (5) allow us to fit our susceptibility data and determine the model parameters. Actually, in the case of powder samples a factor of  $1/3$  has to be included in the right-hand side of the first line in equation (5) due to averaging over the field orientations. We want to emphasize that a careful procedure is needed to achieve trustful fittings. First, we perform a fitting to the Curie-Weiss law,  $\chi = C/(T - \theta_W)$ , in the range of higher temperatures, obtaining highly precise values for the constants  $C$  and  $\theta_W$ . These determine, respectively, the values of the coefficients  $c$  and  $a_1$  of equation (4), which are kept fixed in the subsequent fitting procedure. Next, we adjust the formal susceptibility series typically up to order  $T^{-6}$ , enforcing the above mentioned constraints on  $c$  and  $a_1$ . We assume an effective uniform system, with the spin  $S$  obtained by averaging the corresponding high-spin values for Fe and Co. Finally, using equations (5), we obtain the  $g$ -factor from the adjusted value of  $c$ , and the three exchange constants from the values of  $a_1$ ,  $a_2$  and  $a_3$ . This last step involves numerically solving a system of three non-linear equations, the last three of equations (5).

Fitted values of the exchange constants are shown in figure 6 as functions of the Fe fraction  $x$ . We want to remark that the dominant exchange interaction is  $J_2$ , i.e., the nnn coupling along the easy axis, which is always antiferromagnetic. The other two exchange constants,  $J_1$  and  $J'_2$  have smaller absolute values, and change sign around the concentration  $x = 0.46$ , where the planar spin structure changes from SAF2 to SAF1. These results are in full agreement with the phase diagrams of figure 5. On the other hand, we can see significant changes also near the bicritical point at  $x \simeq 0.01$ . This may reflect the fact that a purely two-dimensional model is not enough to describe the



**Figure 6.** Exchange constants of the model Hamiltonian (3) for varying  $x$  values throughout the  $\text{Fe}_x\text{Co}_{1-x}\text{Ta}_2\text{O}_6$  series, as obtained from fittings of the susceptibility data to the corresponding high-temperature series. Lines between symbols are just guides to the eye.

susceptibility, since in the transition at small  $x$  involves two ordered phases that present the same in-plane magnetic structure.

Concerning the relative intensities of the various exchange couplings as well as the sign change observed for  $J_1$  and  $J'_2$ , it should be noticed that the latter two are related to superexchange paths that are not straight lines, in contrast to  $J_2$ , as can be seen in figure 3. The dependence of exchange constants on bond angles was first demonstrated in the pioneering works of Goodenough [25, 26] and Kanamori [27], for direct cation-cation coupling, and for the case of one intervening anion. Here the situation is still more complex, as there are two intervening anions. In addition, the  $3d-t_{2g}$  manifold has different fillings for Co and Fe, the orbitals tend to have different spatial extents as the ion charge changes, and the crystal-field splitting of these levels is varying with  $x$ , following the evolution of the distortion index of the oxygen octahedra [13]. Even though a microscopic analysis of the relevant superexchange processes has not yet been done, it is possible to infer from figure 3 that different orbitals are involved in the processes determining  $J_2$  with respect to the other two couplings, which could be the origin of the observed differences in sign and strength.

#### 4. Conclusions

In this work, combining information obtained from neutron-diffraction and magnetic-susceptibility measurements, we complemented the  $T$  vs.  $x$  magnetic phase diagram of [13] for the  $\text{Fe}_x\text{Co}_{1-x}\text{Ta}_2\text{O}_6$  series. Coexistence of two distinct magnetic phases was observed around a new bicritical point located near  $x = 0.01$ , similarly to what had been observed around  $x = 0.46$  [13]. All the low-temperature magnetic structures reflect the

presence of a large magnetocrystalline anisotropy, with easy axes that alternate between the  $[110]$  and  $[\bar{1}\bar{1}0]$  directions on neighboring magnetic planes. These directions coincide with the shortened principal axes of oxygen octahedra that surround each magnetic ion. Two in-plane patterns of magnetic moments appear, for Fe-rich and Co-rich samples, but the latter also show two different periodicities along the  $c$  axis, yielding three distinct magnetic phases.

At high temperatures, the paramagnetic susceptibility can be described within a two-dimensional model of exchange-coupled localized spins. In contrast to what was previously done for  $\text{FeTa}_2\text{O}_6$  [2], we introduced two different next-nearest-neighbor exchange interactions (parallel and perpendicular to the anisotropy axis). We calculated the coefficients of the high-temperature series of  $\chi(T)$  up to order  $T^{-4}$  for this new model, using it to fit the paramagnetic susceptibility data. With this we were able to obtain values of the exchange constants which are consistent with the in-plane magnetic structures observed by neutron diffraction.

It is worth noticing that all the low-temperature magnetic phases present well defined periodicities both in the  $ab$  plane and along the  $c$  axis. It is thus clear that, despite the quasi-two-dimensional character of these compounds, they order in three dimensions. The complex magnetic structures observed may result from subtle changes in the intraplane and interplane couplings, within the constraints imposed by a strong magnetic anisotropy with alternating orientations of the easy axes. While the in-plane interactions have been successfully modeled here, progress must still be made in the understanding of interplane coupling. For both of these interactions a detailed analysis of the relevant superexchange processes is also needed in order to provide microscopic justification for the model.

## Acknowledgments

This work was supported in part by the French-Brazilian agreement CAPES-COFECUB and the Brazilian agency CNPq. The authors would also like to thank Claudine Lacroix for interesting discussions. Financial support of the Region Rhone-Alpes (France) via the ARCUS-Br sil cooperation program is also warmly acknowledged.

## References

- [1] Eicher S M, Greedan J E and Lushington K J 1986 *J. Sol. St. Chem.* **62** 220
- [2] Muraoka Y, Idogaki T and Uryu N 1988 *J. Phys. Soc. Jpn.* **57** 1758
- [3] Zawislak L I, da Cunha J B M, Vasquez A and dos Santos C A 1995 *Sol. St. Comm.* **94** 345
- [4] Chung E M L, Lees M R, McIntyre G J, Wilkinson C, Balakrishnan G, Hague J P, Visser D and Paul D M 2004 *J. Phys.: Condens. Matter* **16** 7837
- [5] Hague J P, E. M. Chung E M L, Visser D, Balakrishnan G, Clementyev E, Paul D M and Lees M R 2005 *J. Phys.: Condens. Matter* **17** 7227
- [6] Kremer R K, Greedan J E, Gmelin E, Dai W, White M A, S. Eicher M and Lushington K J 1988 *J. Phys. (France)* **49** 1495

- [7] Ehrenberg H, Wltschek G, Rodriguez-Carvajal J and Vogt T 1988 *J. Magn. Magn. Mater.* **184** 111
- [8] Reimers J N, Greedan J E, Stager C V and Kremer R K 1989 *J. Sol. St. Chem.* **83** 20
- [9] Borromei R, Cavallie E and Oleari L 1993 *Inorg. Chim. Acta* **204** 159
- [10] Kremer R K and Greedan J E 1988 *J. Sol. St. Chem.* **73** 579
- [11] Kinast E J, dos Santos C A, Schmitt D, Isnard O, Gusmão M A and da Cunha J B M 2010 *J. Alloys and Compounds* **491** 44
- [12] Ye J H, Matsushita A and Zou Z G 2003 *Int. J. of Hydrogen Energy* **28** 651
- [13] Kinast E J, Antonietti V, Schmitt D, Isnard O, da Cunha J B M, Gusmão M A and dos Santos C A 2003 *Phys. Rev. Lett.* **91** 19720
- [14] de Oliveira Neto S R, Kinast E J, Gusmão M A, dos Santos C A, Isnard O and da Cunha J B M 2007 *J. Phys.: Condens. Matter* **19** 356210
- [15] Oliveira Neto S R, Kinast E J, Isnard O, da Cunha J B M, Gusmão M A and dos Santos C A 2008 *J. Magn. Magn. Mater.* **320** e125
- [16] Antonietti V, Kinast E J, Zawislak L I, da Cunha J B M and dos Santos C A 2001 *J. Phys. Chem. Solids* **62** 1239
- [17] Barlet A, Genna J C and Lethuillier P 1991 *cryogenic* **31** 801
- [18] Arrott A 1957 *Phys. Rev.* **108** 1394
- [19] Rodriguez-Carvajal J 1993 *Physica B* **192** 55
- [20] McCusker L B, Von Dreele R B, Cox D E, Louer D and Scardi P 1999 *J. App. Cryst.* **32** 36
- [21] Sears V F 1992 *Neutron News* **3** 26
- [22] Bouvier M, Lethuillier P and Schmitt D 1994 *Phys. Rev. B* **50** 13453
- [23] Gignoux D and Schlenker M 2002 *Magnetism I: Fundamentals*, E. du Trémolet de Lacheisserie, Kluwer Academic Press
- [24] Fan C and Wu F Y 1969 *Phys. Rev.* **179** 560
- [25] Goodenough J B 1958 *J. Phys. Chem. Solids* **6** 287
- [26] Goodenough J B 1963 *Magnetism and the Chemical Bond*, Interscience-Wiley
- [27] Kanamori J 1959 *J. Phys. Chem. Solids* **10** 87